

# Real-time economic dispatch for the supply side of the energy-water nexus



Apoorva Santhosh<sup>a</sup>, Amro M. Farid<sup>a,b,\*</sup>, Kamal Youcef-Toumi<sup>c</sup>

<sup>a</sup>Masdar Institute, Engineering Systems & Management, P.O. Box 54224, Abu Dhabi, United Arab Emirates

<sup>b</sup>MIT Technology Development Program, 77 Massachusetts Avenue, Cambridge, MA 02139, United States

<sup>c</sup>MIT Mechanical Engineering, 77 Massachusetts Avenue, Cambridge, MA 02139, United States

## HIGHLIGHTS

- First multi-plant real-time simultaneous economic dispatch of power & water.
- Constrained production cost optimization of energy-water nexus supply side.
- Development is contrasted to single product and power-heat literature.
- Results indicate dual-product plants crowd out cheaper single product plants.
- Directly applicable to regions with integrated water & energy utilities (e.g. GCC).

## ARTICLE INFO

### Article history:

Received 10 June 2013

Received in revised form 27 January 2014

Accepted 29 January 2014

### Keywords:

Energy-water nexus  
Electricity market  
Smart power grid  
Smart water grid  
Water distribution  
Energy management

## ABSTRACT

Clean energy and water are two essential resources that any society must securely deliver. Their usage raises sustainability issues and questions of nations' resilience in face of global changes and mega-trends such as population growth, global climate change, and economic growth. Traditionally, the infrastructure systems that deliver these precious commodities, the water distribution and power transmission networks are thought of as separate, uncoupled systems. However, in reality, they are very much coupled in what is commonly known as the energy-water nexus. Although this subject has recently caught the attention of numerous policy and regulatory agencies, rarely is it holistically addressed in terms of an integrated engineering system for its management, planning, and regulation as an interdisciplinary concern. This work specifically fills this gap by addressing the supply side of this integrated engineering system. Specifically, it develops the multi-plant real-time simultaneous economic dispatch of power and water. While significant background literature has addressed traditional power dispatch, and the emerging co-dispatch of power and heat, as of now there does not exist a parameterized model for the optimized dispatch of power and water for multiple power, water, and coproduction facilities. The work presents such a model where production costs are minimized subject to capacity, demand and process constraints. It is demonstrated on an illustrative example of modest size. Interesting results were observed suggesting that the coproduction minimum capacity limits and process constraints can lead to scenarios where cheaper single product plants can be crowded out of the dispatch. The program provides a systematic method of achieving optimal results and can serve as a basis for set-points upon which individual plants can implement their optimal control. In so doing, it makes a supply-side contribution to the ongoing grand-challenge of improving the sustainability of the energy-water nexus.

© 2014 Elsevier Ltd. All rights reserved.

## 1. Introduction

### 1.1. Motivation

Clean energy and water are two essential resources that any society must securely deliver [1] in order to develop sustainably; i.e. meet its economic, social and environmental goals [2,1,3,4]. In the case of energy, the overuse of conventional resources has

\* Corresponding author at: MIT Technology Development Program, 77 Massachusetts Avenue, Cambridge, MA 02139, United States. Tel.: +1 646 724 0264.

E-mail addresses: [asanthosh@masdar.ac.ae](mailto:asanthosh@masdar.ac.ae) (A. Santhosh), [afarid@masdar.ac.ae](mailto:afarid@masdar.ac.ae), [amfarid@mit.edu](mailto:amfarid@mit.edu) (A.M. Farid), [youcef@mit.edu](mailto:youcef@mit.edu) (K. Youcef-Toumi).

raised concerns over global climate change, smog and acid rain collectively [5]. Consequently, research into clean renewable energy resources and energy efficiency methods has increased. Similarly, potable water is another vital resource for survival and development. Increased water use has grown substantially in recent years; tracking strongly with energy use and economic development and leading to depleted water tables in many geographic regions [6]. Therefore, there is an important need to optimize both energy and water resources in light of quickly depleting global energy resources, increased concern about national security, and the need for sustainable economic growth.

Energy and water usage also raises sustainability issues and questions of nations resilience in the face of global changes and mega-trends [2,6]. Developing nations, in particular, project strong water and electricity demand growth driven by population growth. Economic growth and the associated improvements in individual lifestyles also imply a subsequent intensification in the per capita demand of water and electrical energy. Furthermore, the hot and arid climates found in many developing nations amplify the coupling of water and energy use. As a result, typical water deficits may intensify into aggravated water scarcity. Global climate change projections foresee further distortions in the availability and consumption of fresh water [7]. The nations that take early planning measures in their infrastructure development are likely to be in a better position to mitigate energy and water usage impacts.

## 1.2. Scope

Traditionally water distribution and power transmission networks are thought of as separate uncoupled infrastructure systems. And yet, these two essential resources are intrinsically coupled in that the production, distribution and consumption of one often requires the other [8]. This interlinked meta-system is often called the energy-water nexus and is defined here as:

**Definition 1.** Energy-Water Nexus [9–12]: A system-of-systems composed of one infrastructure system with the artifacts necessary to describe a full energy value chain and another infrastructure system with the artifacts necessary to describe a full water value chain.

Table 1 shows the couplings between the energy and water systems. The greatest attention has been given to the cross-interactions of energy supply to water demand or vice versa. Many empirical methods and studies have attempted to quantitatively assess the water consumption requirements and impacts of thermal power generation facilities [13–21]. Similarly, research is underway to improve technologies that would diminish this impact [22,23]. Another cross-coupling is the electrical pumping energy required to produce and dispatch potable water [24–27]. As the subject of this paper, coproduction facilities like hydroelectric and thermal desalination plants [28] couple the respective supply sides of energy and water [29]. Finally, the residential, commercial, and industrial use of electric heating and cooling for water consumption presents a major coupling on the demand side of both systems [30].

**Table 1**  
Supply and demand side energy-water nexus couplings.

	Power supply	Power demand
Water supply	Co-generation: • Thermal Desalination • Hydroelectric	• Pumped water • Water Distribution • Wastewater Recycling
Water demand	Thermal-power generation facilities	Residential, commercial, industrial use of electric heating & cooling of water

Although the energy-water nexus has recently caught the attention of numerous policy and regulatory agencies [13,24,30–35], rarely [36–38], is it holistically addressed in terms of an integrated engineering system framework for its management, planning and regulation as an interdisciplinary concern. Recent research into smart (power) grid activities implicitly require a rebalancing of power generation technology portfolio [39]. Similarly, smart (water) grid activities implicitly require a rebalancing of the water supply technologies be they desalination, groundwater pumping or water recycling [40,41]. Paradigmatically, as well as technologically, there is a great potential for convergence of these work streams. Recently, the energy-water nexus has been modeled as an integrated engineering system [9,10] and initial work for holistic quantified planning is reported [11,12].

This paper restricts its scope to the real-time economic dispatch of the supply-side of the engineered electricity and water systems. This includes the couplings manifested by the operations management of hydroelectric and thermal desalination facilities. Hydroelectric facilities have a hydro-power production function that ties the output power to the spillage [42–45]. Meanwhile, thermal desalination facilities require a steam balance that couples the heat by-product of power generation to the production of potable water [46–48]. Therefore, in this approach, the optimal mix of produced water and power is determined by how these plants operate within the greater context of water and power real-time economic dispatch. The term “real-time” economic dispatch is borrowed from power system market operation to refer to a time scale that ranges from 5 min to 1 h.

## 1.3. Relevance

The optimization of the supply side coupling is of greatest interest in the Gulf Cooperation Council (GCC) countries. The hot and arid climates found in the GCC cause a heavy reliance on desalination technology to alleviate the scarcity of potable ground water. The additional reliance on climate-controlled buildings further exacerbates power dispatch with sharp peak loads. Fortunately, most GCC nations operate their water and power utilities within a single organization and therefore the optimization program presented in this work is of direct industrial applicability [49]. Similar combined water and power utilities may be found in other regions of the world. Furthermore, the presence of a cooptimization program can highlight potential efficiencies if separated power and water utilities were to coordinate their activities. The cost-optimization program presented in this work is first intended for the GCC region which works under regulated frameworks. Ultimately, this work can serve in the development of an integrated energy-water market not unlike deregulated energy markets found in European and North American nations.

## 1.4. Contribution

This paper constitutes the first part in a three part series in which traditional power system optimization techniques are generalized from power-only markets to the energy-water nexus supply side. The first of these optimization programs is the real-time economic dispatch [50,51]. It is further developed here. Its

optimization program is compact so as to limit computational intensity and facilitate implementation on a time scale between 5 min and 1 h. This work is complemented by an expanded program that includes ramping rates and the storage of both water and energy [52,53]. It closely resembles a power system unit commitment or “look-ahead dispatch”. Finally, the third part in the series introduces the effect of power and water network capacity limits [54]. It closely resemble a power system DC optimal power flow.

### 1.5. Paper outline

The remainder of the paper develops in six sections. Section 2 highlights aspects of the background literature to power-water co-optimization. Specifically, the power economic dispatch problem formulation is introduced as a prerequisite single-product optimization and then the dual-product co-optimization literature is reviewed. The paper then presents the modeling methodology for the co-optimization of power and water and then proceeds to explain the simulation methodology in Section 4. Section 5 presents the results for an example system with 8 plants under three different operating scenarios: uncoupled, coupled-inflexible, coupled-flexible. The paper concludes in Section 6. Given the interdisciplinary nature of the work, a large number of both context and foundational literature has been included.

## 2. Background literature

This section highlights aspects of the background literature for power-water co-optimization. First, power and water economic optimization literature are introduced as prerequisite single product optimizations. Next, the literature on dual product optimization for power and heat is reviewed. The section concludes with the mention of efforts to co-optimize power and water.

### 2.1. Real-time economic dispatch of power – Problem formulation

Economic dispatch [55] is the process of allocating the generation of power in a manner so as to minimize the cost of production of the needed power by encouraging the use of cheap fuels and/or most efficient plants. This is an area which has been developed extensively both academically and industrially [56,57]. One of the most important advantages of the economic dispatch problem is that it allows for all types of generating plants to be treated equally despite their individual physical characteristics and constraints. It does so by focusing on creating a generalized algorithm with a uniform cost function and constraints in order to effectively handle different types of plants. Typically, the cost function is taken to be of quadratic form, however, different approaches also consider the cost to be linear, piecewise linear, and in certain cases of higher polynomials as needed [56,58,59].

Industrially speaking, the economic dispatch of power is usually handled in stages of increasing frequency rather than in a single pass optimization. The first stage is called the day-ahead energy market and uses a class of optimization program called unit commitment. It serves to commit resources, and set approximate generation levels and prices for the 24 h of the following day based upon demand bids, generation offers, and scheduled bilateral transactions [60–71]. The next stage in economic dispatch is the real time spot market [72–77]. In this real-time economic dispatch, electricity generation and prices are calculated at intervals between 5 min and 1 h based upon actual grid operating conditions. This paper may be viewed as a development of a real-time economic dispatch for both power and water. The two stages applied together allow the dispatch to correct for errors in the demand forecast while respecting the startup and ramping capabilities of

the generation facilities [78,79]. Finally, the optimal power flow problem considers the power transmission constraints within the network [80–87].

The implementation of economic dispatch also varies widely depending upon the regulatory structure. They are broadly classified as regulated and unregulated. In the former, although the utility may purchase from a neighboring utility, it is vertically integrated and therefore primarily responsible for its own generation, transmission and distribution of power to the customers in its area. In the deregulated supply system, generation and distribution are uncoupled and customers are no longer bound to one utility but are free to purchase from any suppliers on the grid. Purchasing of power is done via the electricity market mechanisms and transmission scheduling is conducted by the independent system operator [88–90]. Comprehensive treatments of deregulated electricity markets can be found in [91–95], while the literature also provides specialized treatments in deregulated price forecasting, dispatching and bidding simulation [96–98]. It is generally agreed that deregulated power systems provide greater market incentives for generation capacity investments and as a result allow for a smoother transition into newer technologies and greater flexibility [99].

From a purely mathematical point of view, real-time economic dispatch can be considered the most basic algorithm to deliver power in an economic fashion [55]. It minimizes the total power generation cost subject to the capacity limits of the power plants and the balance of power generation and demand under the lossless transmission assumption. It can be presented equivalently as either a primal or dual problem depending on the implementation in a regulated or deregulated market [57]. Formally, the primal problem is:

$$\min C_G(x_{pi}) = \sum_{i=1}^{n_p} C_{pi}(x_{pi}) \quad (1)$$

$$\text{s.t. } \sum_{i=1}^{n_p} (x_{pi}) = D_p \quad (2)$$

$$x_{pi} \leq \bar{x}_{pi} \quad (3)$$

### 2.2. Real-time economic dispatch of municipal water

In contrast to the well developed regulated and deregulated markets within the electrical infrastructure, the economic dispatch of water has achieved neither a comparable intellectual consensus nor widespread industrial adoption. In their recent review, Chong and Sunding outline the broad classes of objections to water markets and trading [100]. That said, the Dublin Principles arising from the 1992 International Conference on Water and Environment state [101]: “Managing water as an economic good is an important way of achieving efficient and equitable use, and of encouraging conservation and protection of water resources.” A number of different economic approaches to water management have emerged including general equilibrium models, cost-benefit analyses, agent-based models, and hydro-economic models [100].

The broader class of hydro-economic models are of greatest relevance here in that they can be considered to incorporate the real-time economic dispatch of water. Hydro-economic models typically use optimization over discrete time-steps to simulate the water resource management of a region. As the name suggests, they combine an economic model in the form of a monetization function of the water's value with algebraic constraints that describe the engineering physics of the water flows in the region [100].

When applied to municipal water, the monetization often reflects the utility's variable costs for water treatment and pumping.

The underlying engineering model depends on the intended application but often includes state-space equations of the hydrodynamics, a connectivity matrix to represent the hydraulic network, and capacity limits on the reservoir sizes and releases [102]. The temporal resolution can range from hours to years and the spatial resolution can range from a household to groups of countries [100,102]. Interestingly, the academic literature concerning the optimal pumping control problem for multi-reservoir systems has drawn extensively from techniques as varied as linear and non-linear programming, stochastic optimization, dynamic programming and discrete-time optimal control [102–112]. As in power systems, multi-stage optimizations in which medium-term operations are cascaded into hourly optimizations have also been reported [113,114]. These may be further cascaded into real-time reservoir control systems [115–117]. In all, there exists a rich academic literature to address the various types of economic dispatch of municipal water.

Nevertheless, these academic contributions have not necessarily translated to industrial implementation [100,102,103]. Significant anecdotal evidence has been reported within the literature over several decades suggesting a lack of industrial confidence in the applicability of the optimization models, combined with poorly designed incentives to improve operational efficiency [100,102,103,118]. That said, the dozen or so successful real-time optimal pumping control implementations have relied on decision support systems and SCADA as enabling technologies. The continued development of these technologies in combination with increasing water scarcity pressures are likely to influence greater adoption of real-time economic dispatch of municipal water [102,103].

### 2.3. Co-dispatch of power and heat

The consistent application of economic dispatch of power over decades has provided a market signal to not just reduce costs but also invest into more energy efficient technologies. In this regard, combined cycle power plants were systematically favored over single cycle facilities. Furthermore, facilities that cogenerated power and heat could demonstrate even higher efficiencies by using heat as a valued product for nearby industrial sectors such as food processing, chemical production, and district heating [119–121]. The resulting efficiency gains also bring about cost savings, reduced air pollution and greenhouse gas emissions, increased power reliability and quality, reduced grid congestion and avoided distribution losses [122]. Many policy-makers, particularly in Northern Europe, further supported dual product facilities through regulatory development [123]. Nevertheless, the technical and economic rationalization of a cogeneration solution often depended on the challenging conditions of having a consistently available, dedicated and co-located heat consumer [124] – often in the form of a contentiously negotiated [125,126] long-term contract [127]. Naturally, some have argued to ease these restrictions on heat and power – as dual products – with a more dynamic treatment [128].

To that effect, a power-heat economic dispatch approach has been applied within the literature. Typically, it creates a single objective function for coproduction plants that is dependent on the amount of power and heat produced. Constraints are then added to set up limits for both power and heat capacities. These limits usually define a feasible region in which the cogeneration plant can operate with respect to power and heat produced [129–133].

### 2.4. Co-optimization of power and water

Generally speaking, research on co-optimization of power and water has focused on the optimization of one particular plant

and hence does not provide an extensible and general optimization formulation. For example, some focus on optimized planning and design rather than operations [134–136]. Still others find methods of cost allocation [137]. Finally, one author directly addresses the economic dispatch of a single MSF desalination facility composed of a number of sub-units but neither generalizes the formulation nor applies it to all the water and production units in the water and power grids [138]. In contrast, a number of robust optimization methods have been recently applied to hydrothermal systems [42,139–144], but they do not specifically include the potable water demand from the water utility. To the authors' knowledge, there does not exist a parametrized model for the optimization of multiple co-generation plants in conjunction with pure power and water plants with no such assumptions of cost splitting. There exists a need for a model that allows for all three plants to be treated with equity. While similar techniques have been used for power-heat cogeneration, it has not been extensively explored in power water co-optimization and may serve as the basis of set point determination for single-plant optimization formulations.

## 3. Modeling methodology

This section describes the modeling methodology for the formulation of an optimization program to simultaneously dispatch power and water. Section 3.1 provides a conceptual model of the system of interest. Section 3.2 then recounts the optimization program first presented in [50] whose goal is to provide dispatch set-points that individual facilities can use for single-plant target optimizations. Recalling the discussion of Section 1.4, the ultimate goal of this optimization program is to mimic the role of a real-time power market but instead for the supply-side of the energy-water nexus. Therefore, efforts are made to keep the optimization program as compact as possible to limit its computational intensity and facilitate its implementation on a time scale between 5 min and 1 h.

### 3.1. Conceptual model

Fig. 1 provides a graphical representation of the conceptual model that serves as the basis for the development of the optimization program. It consists of an integrated power & water utility that is interested in simultaneously serving an electrical power demand as well as a potable water demand. The respective grids are modeled as single nodes. The utility dispatches power, water, and coproduction facilities may be independent or vertically integrated. The power facilities may be taken as dispatchable thermal power generation plants. The coproduction facilities may be either hydroelectric or thermal desalination. They couple the respective grids by virtue of their production cost functions and their process constraints. The water plant may be a ground or surface pumping station or a reverse osmosis desalination plant all with the necessary treatment capabilities to ensure potable water. The conceptual model and associated optimization program do not preclude a wastewater treatment plant from recycling water back into the potable water distribution network, although this remains an infrequent use case.

The choice of three types of facilities includes two inherent assumptions. The optimization programs in [52,53] explicitly considered electrical energy and water storage facilities. Here, it is assumed that electrical energy storage facilities are of such a small penetration that their contribution can be neglected. In contrast, water utilities maintain water storage reservoirs whose volume capacity is often greater than many days worth of maximum flow release. Therefore, within the time scale of 5 min to 1 h, it is highly unlikely that a storage facility will run up against its volume

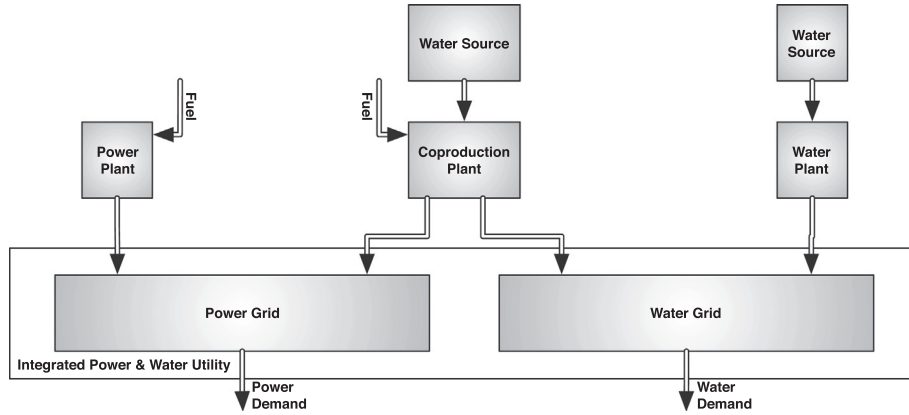


Fig. 1. Model for the co-dispatch of power and water supply.

capacity limit. As a result, it is not essential to include the storage level of water storage facilities over this time scale. Instead, the set of water storage facilities may be included directly within the set of water production facilities. These two assumptions bring about a significant computational benefit in that the optimization time blocks can now be entirely decoupled, and a separate optimization can be run as each time block comes in “real-time”.

The power generation facilities require a fuel source whose cost serves as the basis of the production cost function. The same holds true for the coproduction facilities based upon thermal desalination.

Each water and coproduction facility is assumed to draw from its own independent water source. The model also applies to a single aggregate water source; as in the practical case of the Persian Gulf serving all desalination facilities in the U.A.E. Hydrologically speaking, the water sources are assumed to be able to support the maximum water flow capacities of the water production facilities that they serve. The power and water demands are measured net of any power and water requirements to the dispatched facilities and are ultimately delivered to the utility’s power and water customers.

### 3.2. Problem formulation

The formulation of the power–water co-optimization first proposed in [50] is as follows. Minimize the production cost objective function  $C_G$  with respect to the quantity of power generated by a power plant  $x_{pi}$ , water produced by a water plant  $x_{wj}$ , the power generated by a coproduction plant  $x_{cpk}$  and water produced by a coproduction plant  $x_{cwk}$  in the three types of plants:  $i, j, k$  power, water, and coproduction respectively. The following notations are introduced to vectorize the formulation:  $X_{pi} = [x_{pi}, 0]^T$ ,  $X_{wj} = [0, x_{wj}]^T$ ,  $X_{ck} = [x_{cpk}, x_{cwk}]^T$ ,  $D = [D_p, D_w]^T$

$$\min C_G(X_{pi}, X_{wj}, X_{ck}) = \sum_{i=1}^{n_p} C_{pi}(X_{pi}) + \sum_{j=1}^{n_w} C_{wj}(X_{wj}) + \sum_{k=1}^{n_c} C_{ck}(X_{ck}) \quad (4)$$

subject to the capacity, demand and process constraints in Eqs. (5)–(7) respectively.

$$\begin{aligned} \underline{X}_{pi} &\leq X_{pi} \leq \bar{X}_{pi} \quad \forall i = 1, \dots, n_p \\ \underline{X}_{wj} &\leq X_{wj} \leq \bar{X}_{wj} \quad \forall j = 1, \dots, n_w \\ \underline{X}_{ck} &\leq X_{ck} \leq \bar{X}_{ck} \quad \forall k = 1, \dots, n_c \end{aligned} \quad (5)$$

$$\sum_{i=1}^{n_p} X_{pi} + \sum_{j=1}^{n_w} X_{wj} + \sum_{k=1}^{n_c} X_{ck} = D \quad (6)$$

$$\underline{r}_k \leq \frac{x_{cpk}}{x_{cwk}} \leq \bar{r}_k \quad \forall k = 1, \dots, n_{cp} \quad (7)$$

where  $C_{pi}$ ,  $C_{wj}$ ,  $C_{ck}$  are the scalar cost functions for the  $i$ th power production facility, the  $j$ th water production facility and the  $k$ th coproduction facility. Additionally,  $n_p$ ,  $n_w$ ,  $n_c$  are the numbers of power, water and coproduction facilities respectively.  $r_k^{upper}$  and  $r_k^{lower}$  are upper and lower bounds on the power–water production ratio for the coproduction plants. Here, the process constraints do not model the physical flows of power and water for coproduction facilities, as this would be intractable for all facilities. Instead, they represent the reasonable limits of safe operation of the coproduction process.  $D$  represents the power and water product demand vector. Finally, the conventional overbar and underbar notation is used to reflect minimum and maximum capacity limits. Note that  $\underline{x}_{wj}$  and  $\underline{x}_{cwk}$  are allowed to take on negative values to account for the possibility of water storage in the system.

The cost functions  $C_{pi}$ ,  $C_{wj}$ ,  $C_{ck}$  are assumed to exhibit a quadratic structure in their respective production variables. This is a commonly held assumption for all three types of facilities: thermal power and coproduction facilities [56] and water treatment plants [145].

$$\begin{aligned} C_{pi} &= X_{pi}^T A_{pi} X_{pi} + B_{pi} X_{pi} + K_{pi} \\ C_{wj} &= X_{wj}^T A_{wj} X_{wj} + B_{wj} X_{wj} + K_{wj} \\ C_{ck} &= X_{ck}^T A_{ck} X_{ck} + B_{ck} X_{ck} + K_{ck} \end{aligned} \quad (8)$$

The cost function coefficients are appropriately sized positive constant matrices based upon the heat rate characteristics of their respective production units.

The optimization model as presented may be classified as a nonlinear mathematical program subject to smooth monotonic constraints. With the exception of the process constraints, these constraints are linear. Therefore, this mathematical program is a practical candidate for existing off-the-shelf nonlinear optimization engines and has a high potential for industrial implementation within the time scale of 5 min to 1 h.

## 4. Simulation methodology

Recalling Section 1.5, this real-time economic dispatch is the first in a three part series of optimization programs that have been recently developed [50–54]. In order to demonstrate consistency of approach between these contributions together, the common elements of the simulation methodology and data are used throughout. They are recounted here for clarity and convenience.

The data used to demonstrate this optimization was selected for two reasons: (1) The timing of power and water demand peaks and

troughs is typical in the GCC. (2) The range of the power and water demands is exaggerated to demonstrate the convergence capability of the selected optimization engine. The hypothetical test case is composed of 4 power plants, 3 co-production desalination facilities, and 1 reverse osmosis water plant. The associated plant and cost data is summarized in Table 2. Table 3 includes 24 h of power and water demand data and a single optimization run is done for each of these hours.

Given the relatively well-behaved functional forms of the optimization program, it was sufficient to implement the optimization program with existing optimization engines for the numerical solution. The MATLAB and GAMS languages were used together; the former for data handling and visualization and the latter for optimization. The built-in CONOPT solver was selected for its efficient interior point algorithm for large scale nonlinear optimization problems [146].

**5. Results**

The results of the optimization include: the dispatch levels of power and water in Figs. 2 and 3 respectively, the power to water ratio for the coproduction plants relative to the power and water demand ratio in Fig. 4, and the total costs incurred over the 24 h period in Fig. 5. Each of these figures is discussed in turn.

Figs. 2 and 3 show the power and water generation profiles over the 24 h respectively. The optimization successfully completed in spite of a more than a 4× variation in power demand over the course of the day. These exaggerated peaks and troughs for both power and water represent more demanding optimization conditions than those commonly found in power demand profiles in real life dispatch. The power and water demand profiles are also not necessarily trending together leading to a significant variation in the demanded power to water ratio over the course of the day. These demand profiles were chosen in a manner so as to reflect the common power and water demand profiles observed in real life dispatch. In power demand, the peak is typically in the afternoon, when maximum power is utilized by industrial areas, offices, etc. The lowest levels of power required are typically early in the morning and later on in the evening. Water demand has an early peak for irrigation and domestic use and another peak around midday for industrial & commercial use.

**Table 3**  
Power and water demand data [51–53].

Hour	Power demand (MW)	Water demand (m <sup>3</sup> /h)
1	1250	150
2	1125	130
3	875	100
4	750	150
5	950	200
6	1440	350
7	1500	300
8	1750	200
9	2000	300
10	2250	400
11	2500	500
12	2750	600
13	2875	400
14	3250	400
15	2750	500
16	2500	550
17	2125	550
18	2375	500
19	2250	400
20	1975	350
21	1750	300
22	1625	250
23	1500	200
24	1376	150

Interestingly, the co-production facilities act as units of ‘first-choice’. The single product power and water plants are essentially being used as peaking plants; coming into operation only to meet periods of high demand of their respective products. This occurs for two reasons. First, the heat rate data for the coproduction plants, relatively speaking, has a much more exaggerated downward trend making them more economical to run close to capacity whenever possible. The second becomes apparent from Fig. 4.

Fig. 4 elucidates one cause of the coproduction facilities being used as units of ‘first-choice’. As the power to water demand ratio swings over the course of the day, the cogeneration facilities are not just incentivized to run as close to full capacity as possible but also are constrained by their product ratio process constraint. Internal to a coproduction facility, there exist mass and energy balance laws that fundamentally limit the range of the power to water ratio. In this simulation, these limits of safe operation were set to the typical values of  $4 \leq R \leq 9 \text{ MW/m}^3$ . The figure shows that the

**Table 2**  
Plant and cost data [51–53].

Plant type	Index	Max power capacity (MW)	Max water capacity (m <sup>3</sup> /h)	Min power capacity (MW)	Min water capacity (m <sup>3</sup> /h)	Min product ratio (MW h/m <sup>3</sup> )	Max product ratio (MW h/m <sup>3</sup> )
Power	<i>i</i> <sub>1</sub>	500	0	0	0	–	–
Power	<i>i</i> <sub>2</sub>	400	0	0	0	–	–
Power	<i>i</i> <sub>3</sub>	400	0	0	0	–	–
Power	<i>i</i> <sub>4</sub>	350	0	0	0	–	–
Coproduction	<i>k</i> <sub>1</sub>	800	200	160	30	4	9
Coproduction	<i>k</i> <sub>2</sub>	600	150	120	23	4	9
Coproduction	<i>k</i> <sub>3</sub>	400	100	80	15	4	9
Water	<i>j</i> <sub>1</sub>	0	250	0	0	–	–
<i>Power plant cost coefficients</i>				<i>Water plant cost coefficients</i>			
<i>A</i> <sub>p</sub>	<i>B</i> <sub>p</sub>	<i>C</i> <sub>p</sub>		<i>A</i> <sub>w</sub>	<i>B</i> <sub>w</sub>	<i>C</i> <sub>w</sub>	
2.069e–4	–1.483e–1	5.711e+1		1.816e–2	–7.081	7.374	
3.232e–4	–1.854e–1	5.711e+1					
1.065e–3	–6.026e–1	1.268e+2					
4.222e–4	–2.119e–1	5.711e+1					
<i>Coproduction plant cost coefficients</i>							
<i>A</i> <sub>c11</sub>	<i>A</i> <sub>c12</sub>	<i>A</i> <sub>c22</sub>	<i>B</i> <sub>c1</sub>	<i>B</i> <sub>c2</sub>	<i>C</i> <sub>c</sub>		
4.433e–4	3.546e–3	7.093e–3	–1.106	–4.426	7.374e+2		
7.881e–4	6.305e–3	1.261e–2	–1.475	–5.901	7.374e+2		
1.773e–3	1.419e–2	2.837e–2	–2.213	–8.851	7.374e+2		

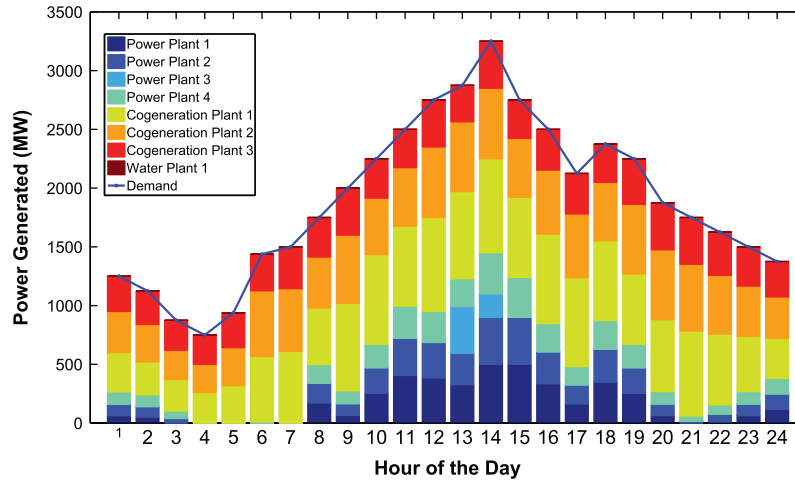


Fig. 2. Power generation and demand profile over 24 h period.

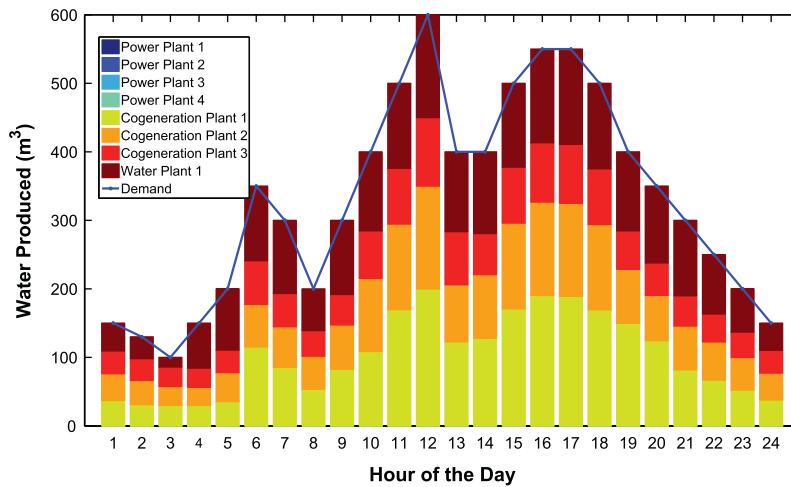


Fig. 3. Water production and demand profile over 24 h period.

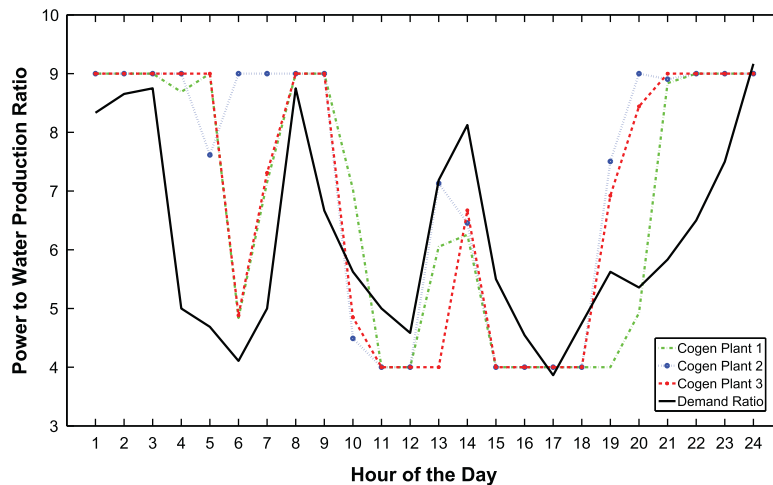


Fig. 4. Power to water ratio for the cogenerator plants.

demand ratio swings significantly causing each of the coproduction facilities to track accordingly. As a result, the single product power and water plants are essentially crowded out; coming online as units of last resort during peak demand hours. The

tracking behavior of the coproduction plants ultimately suggests that any process flexibility that can be achieved by dual product desalination units could lead to significantly improved optima.

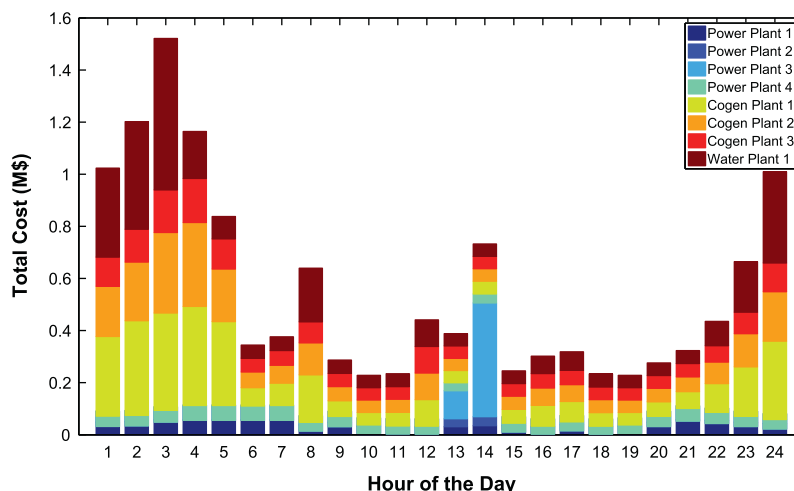


Fig. 5. Cost incurred by different units over the period of 24 h.

Finally, Fig. 5 shows the total costs of generation. At first glance, the results seem counter-intuitive with higher total costs during periods of low production. Once again, this arises from the fact that the coproduction heat rates are higher than single product plants in absolute terms for all production levels and also exhibit a much sharper downward trend for all production levels. As a result, costs are dominated by the coproduction facilities which were only dispatched due to their process constraints. The high cost of low demand arises from the fact that any incremental decreases in demand are more than compensated by increases in the corresponding heat rate.

## 6. Conclusions and future work

The co-optimization program distinguishes itself from previous work in that it allows for deciding set points on the basis of which individual plants can plan their optimal operation. Total costs as a function of power and water generation subject to the demand, capacity and process constraints were minimized on a hypothetical system composed of four power plants, three production facilities and one water plant. Interesting results were observed suggesting that the coproduction minimum capacity limits and process constraints can lead to scenarios where cheaper single product plants can be crowded out of the dispatch. Such results suggest that water and/or power storage can have an important role in relieving process constraints and reducing costs [52,53].

The economic dispatch seeks to optimize the use of resources both in terms of costs and efficiencies. By systematically employing an economic dispatch, there is a trend to dispatch plants that are more energy efficient. Thus, plants are incentivized to improve their efficiencies by using better fuels and better technologies. This is especially relevant for the simultaneous co-optimization of power and water since it encourages more efficient use of fuels by producing dual products while at the same time providing two vital resources in an economical manner. That said, the co-optimization does present challenges that would not be found in either of the single product cases alone.

As has been observed, there has been a strong coupling between water and power and this is more likely to increase in coming years as demand for both increase. There are two ways to handle this. One possible option is to try to reduce coupling between the two products. Water plants based upon reverse osmosis technology do require significant electrical input but they avoid coupling power generation with water production as in MSF plants. How-

ever, this generally is only applicable to new plant installation and much less so to retrofitting scenarios. The other option is to better understand the coupling between these two resources and use a well established algorithm to optimize their production. For example, much attention has recently been given to the integration of renewable energy into desalination facilities [29].

Operations research in the energy-water nexus is an area where there is a lot of potential for future development. As traditional power economic dispatch has evolved over the last few decades, the combined optimization of power and water can evolve similarly. Organic developments that incorporate physical constraints like ramping, transmission losses and start-ups are likely to appear. There is also potential to examine how to better optimize dispatch, by including, for example, power and water storage. Given the ease of water storage and the growing potential for power storage, initial work has been done on the impact of storage facilities on the supply side of energy-water nexus [52,53]. Similarly, initial developments on the incorporation of transmission constraints are reported [51].

## References

- [1] Hoffman AR. *The connection: water and energy security*. Energy Secur 2012.
- [2] US department of energy. US energy sector vulnerabilities to climate change and extreme weather. Technical report. Washington (DC): US Department of Energy, National Renewable Energy Laboratory; 2013.
- [3] Bogardi JJ, Dudgeon D, Lawford R, Flinkerbusch E, Meyn A, Pahl-Wostl C, et al. *Water security for a planet under pressure: interconnected challenges of a changing world call for sustainable solutions*. Curr Opin Environ Sustainab 2012;4:35–43.
- [4] Chester L. *Conceptualising energy security and making explicit its polysemic nature*. Energy Policy 2010;38:887–95.
- [5] IPCC intergovernmental panel on climate change. Climate change 2013: the physical science basis – working group I contribution to the IPCC fifth assessment report. Technical report January 2014. Geneva (Switzerland): IPCC Secretariat; 2013.
- [6] Anonymous-United Nations Education Scientific and Cultural Organization. *Managing water under uncertainty and risk*. Technical report. Paris (France): United Nations Education Scientific and Cultural Organization; 2012.
- [7] IPCC intergovernmental panel on climate change. *Climate change 2007: impacts, adaptation and vulnerability*. Cambridge (MA): Cambridge University Press; 2007.
- [8] Olsson G. *Water and energy: threats and opportunities*. London: IWA Publishing; 2012.
- [9] Lubega WN, Farid AM. A meta-system architecture for the energy-water nexus. In: 8th Annual IEEE systems of systems conference, Maui, Hawaii, USA; 2013. p. 1–6.
- [10] Farid AM, Lubega WN. Powering and watering agriculture: application of energy-water nexus planning. In: IEEE global humanitarian technology conference GHTC 2013, Silicon Valley, CA, USA; 2013. p. 1–6.



- [11] Lubega W, Farid AM. An engineering systems model for the quantitative analysis of the energy-water nexus. In: *Complex systems design & management*, Paris, France; 2013. p. 1–12.
- [12] Lubega WN, Farid AM. A meta-system architecture for the energy-water nexus. *IEEE Syst J* 2014; 1–10 [in Press].
- [13] Macknick J, Barcel J, Codina E, Casas J, Ferrer JL, Garca D, et al. A review of operational water consumption and withdrawal factors for electricity generating technologies. Technical report NREL/TP-6A20-5090. Golden (CO): National Renewable Energy Laboratory; 2011.
- [14] Macknick J, Sattler S, Averyt K, Clemmer S, Rogers J. The water implications of generating electricity: water use across the United States based on different electricity pathways through 2050. *Environ Res Lett* 2012;7:045803.
- [15] Grubert Ea, Beach FC, Webber ME. Can switching fuels save water? A life cycle quantification of freshwater consumption for Texas coal- and natural gas-fired electricity. *Environ Res Lett* 2012;7:045801.
- [16] van Vliet MTH, Vögele S, Rübhelke D. Water constraints on European power supply under climate change: impacts on electricity prices. *Environ Res Lett* 2013;8:035010.
- [17] Miara A, Vörösmarty CJ, Stewart RJ, Wollheim WM, Rosenzweig B. Riverine ecosystem services and the thermoelectric sector: strategic issues facing the Northeastern United States. *Environ Res Lett* 2013;8:025017.
- [18] Stewart RJ, Wollheim WM, Miara A, Vörösmarty CJ, Fekete B, Lammers RB, et al. Horizontal cooling towers: riverine ecosystem services and the fate of thermoelectric heat in the contemporary Northeast US. *Environ Res Lett* 2013;8:025010.
- [19] Madden N, Lewis A, Davis M. Thermal effluent from the power sector: an analysis of once-through cooling system impacts on surface water temperature. *Environ Res Lett* 2013;8:035006.
- [20] Rogers J, Averyt K, Clemmer S, Davis M, Flores-Lopez F, Kenney D, et al. Water-smart power: strengthening the U.S. electricity system in a warming world. Technical report. Cambridge (MA): Union of Concerned Scientists; 2013.
- [21] Allen NSA, Donohoo P, Stillwell AS, King CW, Webster MD, Webber ME, et al. Using market-based dispatching with environmental price signals to reduce emissions and water use at power plants in the Texas grid. *Environ Res Lett* 2011;6:44018.
- [22] Pate R, Hightower M, Cameron C, Einfeld W. Overview of energy-water interdependencies and the emerging energy demands on water resources. Technical report. Albuquerque (NM): Sandia National Laboratories; 2007.
- [23] Macknick J, Newmark R, Heath G, Hallett KC. Operational water consumption and withdrawal factors for electricity generating technologies: a review of existing literature. *Environ Res Lett* 2012;7:045802.
- [24] Griffiths-Sattenspiel B, Wilson W. The carbon footprint of water. Technical report. Portland (OR): River Network; 2009.
- [25] Scott CA. Electricity for groundwater use: constraints and opportunities for adaptive response to climate change. *Environ Res Lett* 2013;8:035005.
- [26] Averyt K, Macknick J, Rogers J, Madden N, Fisher J, Meldrum J, et al. Water use for electricity in the United States: an analysis of reported and calculated water use information for 2008. *Environ Res Lett* 2013;8:015001.
- [27] Meldrum J, Nettles-Anderson S, Heath G, Macknick J. Life cycle water use for electricity generation: a review and harmonization of literature estimates. *Environ Res Lett* 2013;8:015031.
- [28] El-Nashar AM. Cogeneration for power and desalination – state of the art review. *Desalination* 2001;134:7–28.
- [29] Cipollina A, Micale G, Rizzuti L. Seawater desalination: conventional and renewable energy processes. Berlin; London: Springer; 2009.
- [30] Thirlwell GM, Madramootoo CA, Heathcote IW. Energy-water nexus: energy use in the municipal, industrial, and agricultural water sectors. In: *Canada-US water conference*. Washington (DC): Policy Research Initiative of Canada and the Woodrow Wilson Institute; 2007. p. 1–16.
- [31] EPA. Cooling water intake structures at existing facilities and phase I facilities; 2012.
- [32] DOE. Demands on water resources: report to congress on the interdependency of energy and water. Technical report NREL/TP-6A20-5090, Washington, DC.
- [33] WEF. Energy vision update 2009 thirsty energy: water and energy in the 21st century. Technical report. Geneva (Switzerland): World Economic Forum; 2009.
- [34] Jain CP. Water for energy. Technical report. London (United Kingdom): World Energy Council; 2010.
- [35] AWE-ACEEE. Addressing the energy-water nexus: a blueprint for action and policy agenda. AWE-ACEEE; 2011. p. 1–16.
- [36] GAO. Fresh water supply: states views of how federal agencies could help them meet the challenges of expected shortages. Technical report. Washington (DC): United States General Accounting Office; 2003.
- [37] Tidwell VC, Kobos PH, Malczynski L, Klise G, Hart WE, Castillo C. Decision support for integrated water-energy planning. Technical report October. SANDIA National Lab; 2009.
- [38] Sattler S, Macknick J, Yates D, Flores-Lopez F, Lopez A, Rogers J. Linking electricity and water models to assess electricity choices at water-relevant scales. *Environ Res Lett* 2012;7:045804.
- [39] Kassakian JG, Schmalensee R, Desgroseilliers G, Heidel TD, Afridi K, Farid AM. The future of the electricity grid: an interdisciplinary MIT study. Technical report. Cambridge (MA): MIT; 2011.
- [40] Walski TM, Haestad Methods Inc. Advanced water distribution modeling and management. Exton (PA): Bentley Institute Press; 2007.
- [41] Velickov S. Improving efficiency of water systems: practical examples. In: *Arabian water and power forum*, September, Dubai, UAE. p. 1–75.
- [42] Soroudi A. Robust optimization based self scheduling of hydro-thermal Genco in smart grids. *Energy* 2013;61:1–10 [in press].
- [43] Conejo AJ, Arroyo JM, Contreras J, Villamor FA. Self-scheduling of a hydro producer in a pool-based electricity market. *IEEE Trans Power Syst* 2002;17:1265–72.
- [44] Diniz AL, Maceira MEP. A four-dimensional model of hydro generation for the short-term hydrothermal dispatch problem considering head and spillage effects. *IEEE Trans Power Syst* 2008;23:1298–308.
- [45] Basu M. An interactive fuzzy satisfying method based on evolutionary programming technique for multiobjective short-term hydrothermal scheduling. *Electr Power Syst Res* 2004;69:277–85.
- [46] Cipollina A, Micale G, Rizzuti L. Seawater desalination: conventional and renewable energy processes. Berlin; London: Springer; 2009.
- [47] Mezher T, Fath H, Abbas Z, Khaled A. Techno-economic assessment and environmental impacts of desalination technologies. *Desalination* 2011;266:263–73.
- [48] El-Nashar AM. Cogeneration for power and desalination – state of the art review. *Desalination* 2001;134:7–28.
- [49] Anonymous. Abu Dhabi water & electricity company statistical report 1998–2012. Technical report. Abu Dhabi (UAE): Abu Dhabi Water & Electricity Company; 2012.
- [50] Santhosh A, Farid AM, Adegebe A, Youcef-Toumi K. Simultaneous co-optimization for the economic dispatch of power and water networks. In: *The 9th IET international conference on advances in power system control, operation and management*, Hong Kong, China; 2012. p. 1–6.
- [51] Santhosh A. Optimized real time dispatch of generation in power and water Networks. Master's thesis. Masdar Institute; 2013.
- [52] Santhosh A, Farid AM, Youcef-Toumi K. The impact of storage facility capacity and ramping capabilities on the supply side of the energy-water nexus. *Energy* 2014;1–10. <http://dx.doi.org/10.1016/j.energy.2014.01.031>. [in press].
- [53] Santhosh A, Farid AM, Youcef-Toumi K. The impact of storage facilities on the simultaneous economic dispatch of power and water networks limited by ramping rates. In: *IEEE international conference on industrial technology*, Cape Town, South Africa; 2013. p. 1–6.
- [54] Santhosh A, Farid AM, Youcef-toumi K. Optimal network flow for the supply side of the energy-water nexus. In: *2013 IEEE international workshop on intelligent energy systems*, Vienna, Austria. pp. 1–6.
- [55] Kirchmayer LK. Economic operation of power systems. NY: Wiley; 1958.
- [56] Wood AJ, Wollenberg BF, Wood AJ. Power generation, operation, and control. 2nd ed. NY: J. Wiley & Sons; 1996.
- [57] Gómez Expósito A, Conejo AJ, Canizares C. Electric energy systems: analysis and operation. Boca Raton (FL): CRC; 2008.
- [58] Ongsakul W. Real-time economic dispatch using merit order loading for linear decreasing and staircase incremental cost functions. *Electr Power Syst Res* 1999;51:167–73.
- [59] Wu L. A tighter piecewise linear approximation of quadratic cost curves for unit commitment problems. *IEEE Trans Power Syst* 2011;26:2581–3.
- [60] Sheble GB, Fahd GN. Unit commitment literature synopsis. *IEEE Trans Power Syst* 1994;9:128–35.
- [61] Sen S, Kothari DP. Optimal thermal generating unit commitment: a review. *Int J Electr Power Energy Syst* 1998;20:443–51.
- [62] Hobbs BF, Rothkopf MH, O'Neill RP, Chao H-P. The next generation of electric power unit commitment models. New York (NY, USA): Kluwer Academic Publishers; 2001.
- [63] Padhy NP. Unit commitment problem under deregulated environment-a review. In: *Power engineering society general meeting*, 2013. IEEE, vol. 2; 2003. p. 1094.
- [64] Padhy NP. Unit commitment-a bibliographical survey. *IEEE Trans Power Syst* 2004;19:1196–205.
- [65] Das D, Wollenberg BF. Risk assessment of generators bidding in day-ahead market. *IEEE Trans Power Syst* 2005;20:416–24.
- [66] Philpott AB, Pettersen E. Optimizing demand-side bids in day-ahead electricity markets. *IEEE Trans Power Syst* 2006;21:488–98.
- [67] Asir Rajan CC. Hydro-thermal unit commitment problem using simulated annealing embedded evolutionary programming approach. *Int J Electr Power Energy Syst* 2011;33:939–46.
- [68] Xie L, Carvalho PMS, Ferreira L, Liu J, Krogh BH, Popli N, et al. Wind integration in power systems: operational challenges and possible solutions. *Proc IEEE* 2011;99:214–32.
- [69] Bhardwaj A, Kamboj VK, Shukla VK, Singh B, Khurana P. Unit commitment in electrical power system-a literature review. In: *IEEE international power engineering and optimization conference (PEDCO)* Melaka, Malaysia; 2012. p. 275–80.
- [70] Aghaei J, Ahmadi A, Shayanfar HA, Rabiee A. Mixed integer programming of generalized hydro-thermal self-scheduling of generating units. *Electr Eng* 2013;95:109–25.
- [71] Saravanan B, Das S, Sikri S, Kothari DP. A solution to the unit commitment problem—a review. *Front Energy* 2013;7:223–36.
- [72] Chowdhury BH, Rahman S. A review of recent advances in economic dispatch. *IEEE Trans Power Syst* 1990;5:1248–59.
- [73] Yamin HY. Review on methods of generation scheduling in electric power systems. *Electr Power Syst Res* 2004;69:227–48.
- [74] Mahor A, Prasad V, Rangnekar S. Economic dispatch using particle swarm optimization: a review. *Renew Sust Energy Rev* 2009;13:2134–41.

- [75] Boqiang R, Chuanwen J. A review on the economic dispatch and risk management considering wind power in the power market. *Renew Sust Energy Rev* 2009;13:2169–74.
- [76] Xia X, Elaiw AM. Optimal dynamic economic dispatch of generation: a review. *Electr Power Syst Res* 2010;80:975–86.
- [77] Kopsakangas Savolainen M, Svento R. Real-time pricing in the nordic power markets. *Energy Econ* 2012;34:1131–42.
- [78] Boogert A, Dupont D. On the effectiveness of the anti-gaming policy between the day-ahead and real-time electricity markets in The Netherlands. *Energy Econ* 2005;27:752–70.
- [79] Arciniegas Rueda IE, Marathe A. Important variables in explaining real-time peak price in the independent power market of Ontario. *Utilities Policy* 2005;13:27–39.
- [80] Huneault M, Galiana FD. A survey of the optimal power flow literature. *IEEE Trans Power Syst* 1991;6:762–70.
- [81] Momoh JA, Adapa R, El-Hawary ME. A review of selected optimal power flow literature to 1993. I. Nonlinear and quadratic programming approaches. *IEEE Trans Power Syst* 1999;14:96–104.
- [82] Momoh JA, El-Hawary ME, Adapa R. A review of selected optimal power flow literature to 1993. II. Newton, linear programming and interior point methods. *IEEE Trans Power Syst* 1999;14:105–11.
- [83] da Costa G, Costa C, de Souza A. Comparative studies of optimization methods for the optimal power flow problem. *Electr Power Syst Res* 2000;56:249–54.
- [84] Abdel-Moamen MA-R, Padhy NP. Optimal power flow incorporating FACTS devices – bibliography and survey BT – 2003 IEEE PES transmission and distribution conference, September 7, 2003–September 12, 2003. In: Proceedings of the IEEE power engineering society transmission and distribution conference, vol. 2. Roorkee 247667 (India); Institute of Electrical and Electronics Engineers Inc., Department of Electrical Engineering, Indian Institute of Technology; 2003. p. 669–76.
- [85] Pandya KS, Joshi SK. A survey of optimal power flow methods. *J Appl Inform Technol* 2005;4:450–8.
- [86] Qiu Z, Deconinck G, Belmans R. A literature survey of Optimal Power Flow problems in the electricity market context. In: Power systems conference and exposition, 2009. PSCE '09. IEEE/PES, 2009 IEEE/PES power systems conference and exposition, PSCE 2009. IEEE Computer Society, Department of Electrical Engineering, KUL; 2009. p. 1–6.
- [87] Frank S, Rebennack S. A primer on optimal power flow: theory, formulation, and practical examples; 2012.
- [88] Hogan WW. Multiple market-clearing prices, electricity market design and price manipulation. *Electr J* 2012;25:18–32.
- [89] Hogan W. Electricity market restructuring: reforms of reforms. *J Regul Econ* 2002;21:103–32.
- [90] Hogan WW. Electricity whole-sale market design in a low-carbon future. In: Harnessing renewable energy in electric power systems: theory, practice, policy. Washington (DC): RFF Press; 2010. p. 113–36.
- [91] Chao H-P, Huntington HG. Designing competitive electricity markets. Boston (MA): Kluwer Academic; 1998.
- [92] Sheblé GB. Computational auction mechanisms for restructured power industry operation. Boston: Kluwer; 1999.
- [93] Ilic MD, Galiana FD, Fink LH. Power systems restructuring: engineering and economics. Boston: Kluwer Academic Publishers; 1998.
- [94] Kirschen DS, Strbac G. Fundamentals of power system economics. Chichester (West Sussex, England); Hoboken (NJ): John Wiley & Sons; 2004.
- [95] Shahidehpour M, Li Z. Electricity market economics. NY: John Wiley and Sons; 2005.
- [96] Ragupathi R, Das TK. A stochastic game approach for modeling wholesale energy bidding in deregulated power markets. *IEEE Trans Power Syst* 2004;19:849–56.
- [97] Shrestha GB, Song K, Goel L. Strategic self-dispatch considering ramping costs in deregulated power markets. *IEEE Trans Power Syst* 2004;19:1575–81.
- [98] Careri F, Genesi C, Marannino P, Montagna M, Rossi S, Siviero I. Strategic bidding in a day-ahead market by coevolutionary genetic algorithms. In: Power and energy society general meeting. IEEE; 2010. p. 1–8.
- [99] Perez-Arriaga IJ. Managing large scale penetration of intermittent renewables. In: MITEI symposium; 2011.
- [100] Harou JJ, Pulido-Velazquez M, Rosenberg DE, Medellín-Azuara J, Lund JR, Howitt RE. Hydro-economic models: Concepts, design, applications, and future prospects. *J Hydrol* 2009;375:627–43.
- [101] Anonymous-United-Nations. The Dublin statement on water and sustainable development. In: United nations international conference on water and sustainable development, Dublin, Ireland; 1992. p. 1–5.
- [102] Labadie JW. Optimal operation of multireservoir systems: state-of-the-art review. *J Water Resour Plann Manage* 2004;130:93–111.
- [103] Ormsbee LE, Lansley KE. Optimal control of water supply pumping systems. *J Water Resour Plann Manage* 1994;120:237–52.
- [104] Singh A. An overview of the optimization modelling applications. *J Hydrol* 2012;466–467:167–82.
- [105] Hossain MS, El-shafie A. Intelligent systems in optimizing reservoir operation policy: a review. *Water Resour Manage* 2013;27:3387–407.
- [106] Buras N. Scientific allocation of water resources; water resources development and utilization—a rational approach. NY: American Elsevier Pub. Co.; 1972.
- [107] Hall WA, Dracup JA. Water resources systems engineering. NY: McGraw-Hill; 1970.
- [108] Loucks DP, Stedinger JR, Haith DA. Water resource systems planning and analysis. Englewood Cliffs (NJ): Prentice-Hall; 1981.
- [109] Maass A. Design of water-resource systems; new techniques for relating economic objectives, engineering analysis, and governmental planning. Cambridge: Harvard University Press; 1962.
- [110] Mays LW. Hydrosystems engineering and management. Englewood: Water Resources Publications Co.; 2002.
- [111] ReVelle C. Optimizing reservoir resources: including a new model for reservoir reliability. NY: Wiley; 1999.
- [112] Wurbs RA. Modeling and analysis of reservoir system operations. Upper Saddle River (NJ): Prentice Hall PTR; 1996.
- [113] Becker L, Yeh W-G. Optimization of real time operation of a multiple-reservoir system. *Water Resour Res* 1974;10:1107–12.
- [114] Divi R, Ruiu D. Optimal management of multi-purpose reservoirs in a hydro-thermal power system BT – computerized decision support systems for water managers. In: Proceedings of the 3rd water resources operations management workshop, June 27, 1988–June 30, 1988. Canada: Publ by ASCE, SaskPower; 1988. p. 413–872627179.
- [115] Labadie JW, Lazaro RC, Morrow DM. Worth of short-term rainfall forecasting for combined sewer overflow control. *Water Resour Res* 1981;17:1489–97.
- [116] Mishalani NR, Palmer RN. Forecast uncertainty in water supply reservoir operation. *Water Resour Bull* 1988;24:1237–45.
- [117] Georgakakos AP. Value of streamflow forecasting in reservoir operation. *Water Resour Bull* 1989;25:789–800.
- [118] Shepherd A, Ortolano L. Water-supply system operations: critiquing expert-system approach. *J Water Resour Plann Manage* 1996;122:348–55.
- [119] Kiameh P. Power generation handbook: fundamentals of low-emission, high-efficiency power plant operation. 2nd ed. NY: McGraw-Hill; 2012.
- [120] Tsai W-T, Hsien K-J. An analysis of cogeneration system utilized as sustainable energy in the industrial sector in Taiwan. *Renew Sust Energy Rev* 2007;11:2104–20.
- [121] Ziebk A, Gladysz P. Optimal coefficient of the share of cogeneration in district heating systems. *Energy* 2012;45:220–7.
- [122] Rosen MA. Energy, environmental, health and cost benefits of cogeneration from fossil fuels and nuclear energy using the electrical utility facilities of a province. *Energy Sust Develop* 2009;13:43–51.
- [123] EIIPCB-TWIG. Integrated pollution prevention and control (IPPC) reference document on best available techniques for large combustion plants. Technical report. Sevilla (Spain): European IPPC Bureau Technical Working Group – European Commission; 2006.
- [124] Chertow MR, Lombardi DR. Quantifying economic and environmental benefits of co-located firms. *Environ Sci Technol* 2005;39:6535–41.
- [125] Romagnoli PL. Pricing criteria for steam sale contracts. In: Proceedings world geothermal congress, Florence, Italy; 1995. p. 1–4.
- [126] Ibrahim HD, Artono ART. The competitiveness of geothermal power as seen by steam producer, power producer and electricity buyer. In: Proceedings of the world geothermal congress 2005, April, Antalya, Turkey; 2005. p. 1–5.
- [127] Humphrey RL, Parr CJ. Geothermal sales contracts. *Nat Resour Law* 1982;6:13–34.
- [128] Greenwald SF, Gray JP. QF contracts and 21st-century economics. *Power* 2010:26.
- [129] Algie C, Kit Po W. A test system for combined heat and power economic dispatch problems. In: Proceedings of the 2004 IEEE international conference on electric utility deregulation, restructuring and power technologies (DRPT 2004), Hong Kong, vol. 1; 2004. p. 96–101.
- [130] Piperagkas GS, Anastasiadis AG, Hatzigiorgianni ND. Stochastic PSO-based heat and power dispatch under environmental constraints incorporating CHP and wind power units. *Electr Power Syst Res* 2011;81:209–18.
- [131] Tao G, Henwood MI, van Ooijen M. An algorithm for combined heat and power economic dispatch. *IEEE Trans Power Syst* 1996;11:1778–84.
- [132] Linkevics O, Sauhats A. Formulation of the objective function for economic dispatch optimisation of steam cycle CHP plants. In: Power tech, 2005 IEEE Russia; 2005. p. 1–6.
- [133] Rifaat RM. Economic dispatch of combined cycle cogeneration plants with environmental constraints. In: Proceedings of EMPD '98. 1998 international conference on energy management and power delivery, vol. 1; 1998. p. 149–53.
- [134] Ali M E-N. Optimal design of a cogeneration plant for power and desalination taking equipment reliability into consideration. *Desalination* 2008;229:21–32.
- [135] Cardona E, Piacentino A. Optimal design of cogeneration plants for seawater desalination. *Desalination* 2004;166:411–26.
- [136] Shakib SE, Hosseini SR, Amidpour M, Aghanajafi C. Multi-objective optimization of a cogeneration plant for supplying given amount of power and fresh water. *Desalination* 2012;286:225–34.
- [137] Ali M E-N. Cost allocation in a cogeneration plant for the production of power and desalted water – comparison of the exergy cost accounting method with the WEA method. *Desalination* 1999;122:15–34.
- [138] El-nashar AM, Khan MS. Economic scheduling of the UAN cogeneration plant: a preliminary optimization study. *Desalination* 1991;85:93–127.
- [139] Zhang H, Zhou J, Fang N, Zhang R, Zhang Y. Daily hydrothermal scheduling with economic emission using simulated annealing technique based multi-objective cultural differential evolution approach. *Energy* 2013;50:24–37.
- [140] Basu M. Artificial immune system for fixed head hydrothermal power system. *Energy* 2011;36:606–12.

- [141] Catalão JPS, Pousinho HMI, Contreras J. Optimal hydro scheduling and offering strategies considering price uncertainty and risk management. *Energy* 2012;37:237–44.
- [142] Catalão JPS, Pousinho HMI, Mendes VMF. Hydro energy systems management in Portugal: profit-based evaluation of a mixed-integer nonlinear approach. *Energy* 2011;36:500–7.
- [143] Wang Y, Zhou J, Mo L, Zhang R, Zhang Y. Short-term hydrothermal generation scheduling using differential real-coded quantum-inspired evolutionary algorithm. *Energy* 2012;44:657–71.
- [144] Narang N, Dhillon JS, Kothari DP. Multiobjective fixed head hydrothermal scheduling using integrated predator-prey optimization and Powell search method. *Energy* 2012;47:237–52.
- [145] Wu EM-Y. Optimal design of the water treatment plants. In: *Water treatment*. Intech Open Access Publisher; 2013. p. 13–32.
- [146] Drud A. Conopt. Technical report. Bagsvaerd (Denmark): ARKI Consulting and Development A/S; 2013.